Math III\Trigonometry Review

F.TF.1, 2, 5, & 8

Trig Ratios

$Sin\theta = \frac{Opposite}{Hypotenuse}$ $\quad Csc\theta = \frac{Hypotenuse}{Opposite}$

$Cos\theta = \frac{Adjacent}{Hypotenuse}$ $\quad Sec\theta = \frac{Hypotenuse}{Adjacent}$

$Tan\theta = \frac{Opposite}{Adjacent}$ $\quad Cot\theta = \frac{Adjacent}{Opposite}$

Trig Identities

$Tan\theta = \frac{\sin\theta}{\cos\theta}$ $\quad Cot\theta = \frac{\cos\theta}{\sin\theta}$

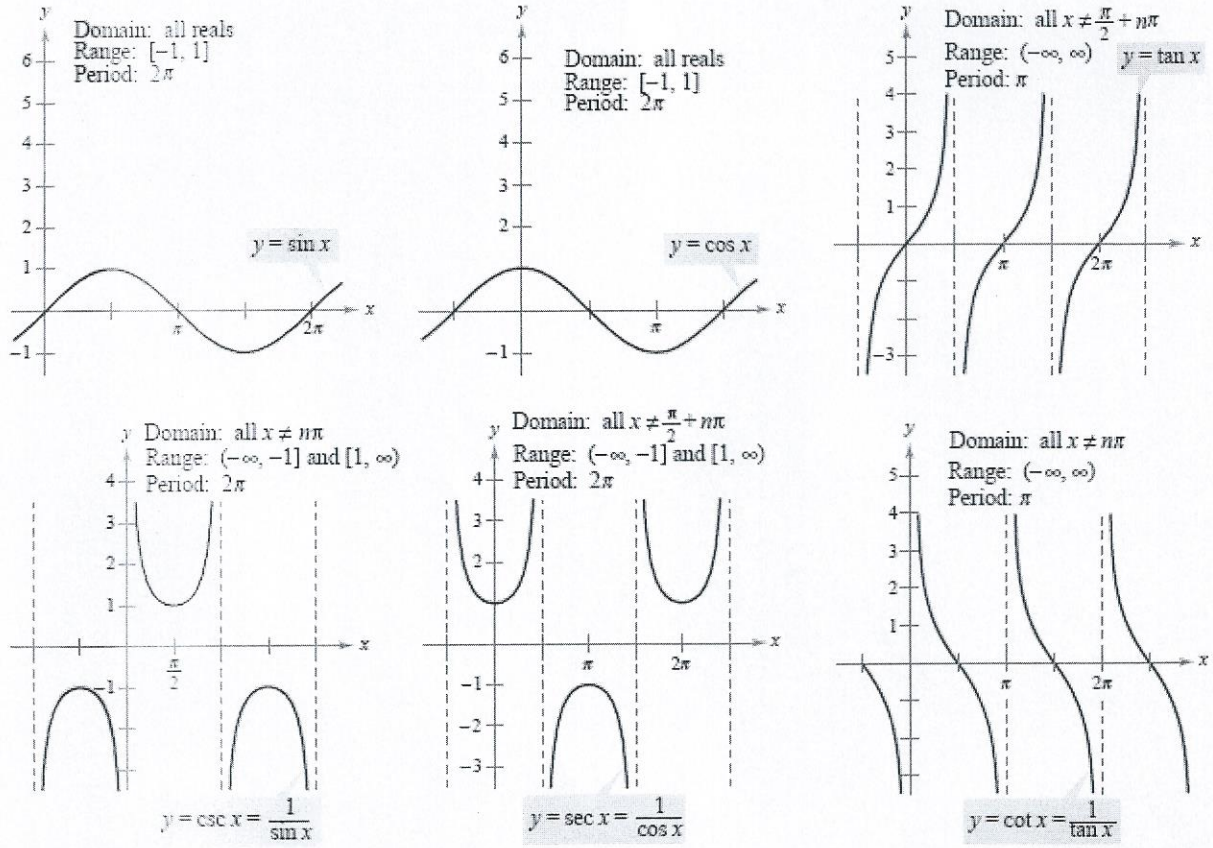
$\csc\theta = \frac{1}{\sin\theta}$ $\quad \sin\theta = \frac{1}{\csc\theta}$

$\sec\theta = \frac{1}{\cos\theta}$ $\quad \cos\theta = \frac{1}{\sec\theta}$

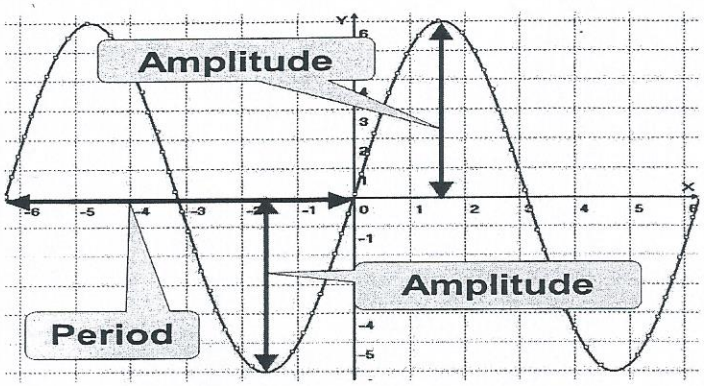
$\cot\theta = \frac{1}{\tan\theta}$ $\quad \tan\theta = \frac{1}{\cot\theta}$

$\sin^2\theta + \cos^2\theta = 1$

Trig Graphs



The graphs of the six trigonometric functions



Amplitude - half of the distance from the maximum and minimum

Period – The horizontal length of one complete cycle

Frequency – The number of cycles the function completes in a given interval.

Midline – The horizontal line half way between the maximum and minimum.

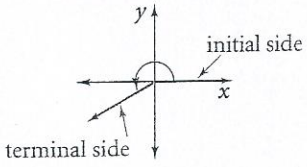
Graph Trigonometric Functions

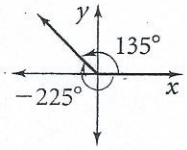
$$y = a \sin b(\theta - h) + k$$

amplitude: a — period: b — phase shift: h — vertical shift: k

Coterminal angles – two angles in standard position that have the same terminal side.

Standard Position





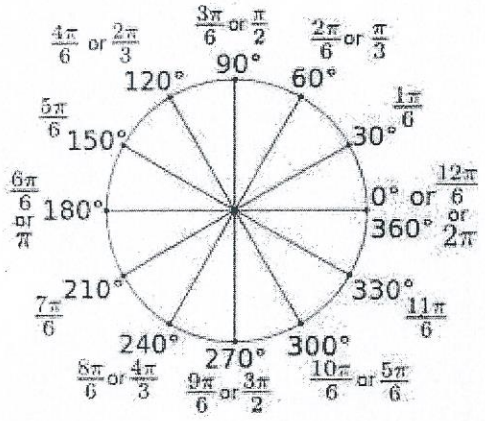
Angles that have measures 135° and −225° are coterminal.

1 radian $\approx 57^0$

To change from degrees to radians – multiply the degrees by $\frac{\pi}{180}$

To change from radians to degrees – multiply the radian by $\frac{180}{\pi}$

Unit Circle



Review Problems

1. Which expression is equivalent to $\sin\theta \cos\theta \csc\theta$?
   A. $\sin\theta$ B. $\cos\theta$ C. $\sec\theta$ D. $\tan\theta$

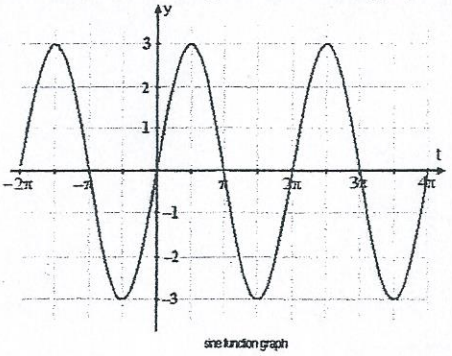
2. Which expression is equivalent to $\cos\theta + \tan\theta \sin\theta$?
   A. $\sec\theta$ B. $\tan\theta$ C. $\sin\theta$ D. $\cos\theta$

3. Which expression is equivalent to $\frac{\cos\theta}{1-\sin\theta} - \tan\theta$?
   A. $\sec\theta$ B. $\sin\theta$ C. $\cos\theta$ D. $\csc\theta$

4. William put the tip of his pencil on the outer edge of a graph of the unit circle at the point (0, -1). He moved this pencil tip through an angle of $\frac{4\pi}{3}$ radians in the counterclockwise direction along the edge of the circle. At what angle of the unit circle did William's pencil tip stop?

A. $\frac{\pi}{3}$ B. $\frac{5\pi}{6}$ C. $\frac{7\pi}{6}$ D. $\frac{5\pi}{3}$

5. Which of the following functions is graphed below?



sine function graph

A. $y = 3\cos\theta$ B. $y = 3\sin\theta$ C. $y = \cos 3\theta$ D. $y = \sin 3\theta$

6. A Ferris wheel has a diameter of 114 feet and is 5 feet off the ground. After a person gets on the bottom car, the Ferris wheel rotates 170^0 counterclockwise before stopping. How high above the ground is the car when it has stopped?

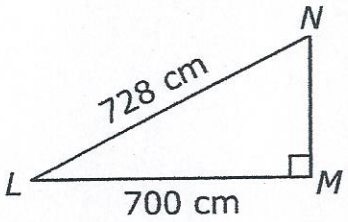
A. 56 feet B. 62 feet C. 80 feet D. 118 feet

7. A Ferris wheel has a radius of 30 meters and is 5 meters off the ground. If a person on the Ferris wheel is 50 meters above the ground, at what degree(s) had the Ferris wheel rotated counterclockwise?

8. A rope is attached to the top of a 25-foot pole. The pole is perpendicular to the ground. Approximately how far from the base of the pole must the rope be attached to make a 30^0 angle with the ground?

A. 12.5 feet B. 14.4 feet C. 43.3 feet D. 50.0 feet

9. In right triangle *LMN*, *LN* = 728 cm and *LM* = 700 cm.



What is the ***approximate*** measure of $\angle NLM$?

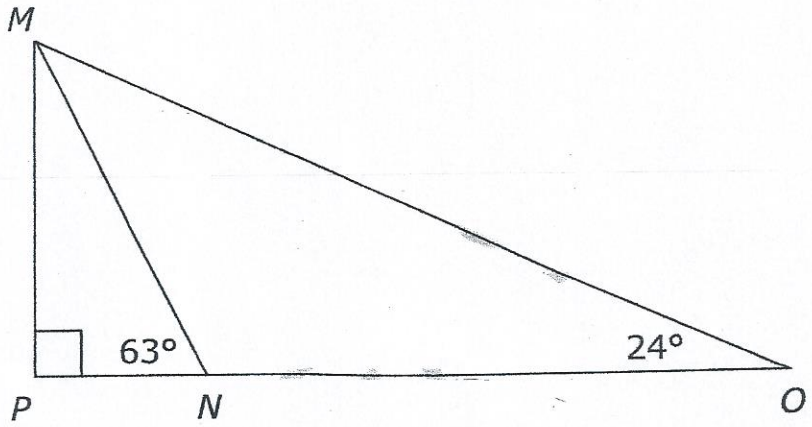
A 15.9°

B 16.6°

C 73.4°

D 74.1°

10. In the diagram below, Triangle *MPO* is a right triangle and $\overline{PN} = 24$ ft.



- What is the length of $\overline{MP}$?
- How much longer is $\overline{MO}$ than $\overline{NM}$?
- How far is point *O* from point *N*?

11. Which expression is equivalent to $\frac{sin^4(\theta)-cos^4(\theta)}{sin^2(\theta)-sin^2(\theta)}$, where $sin^2(\theta) \neq cos^2(\theta)$?

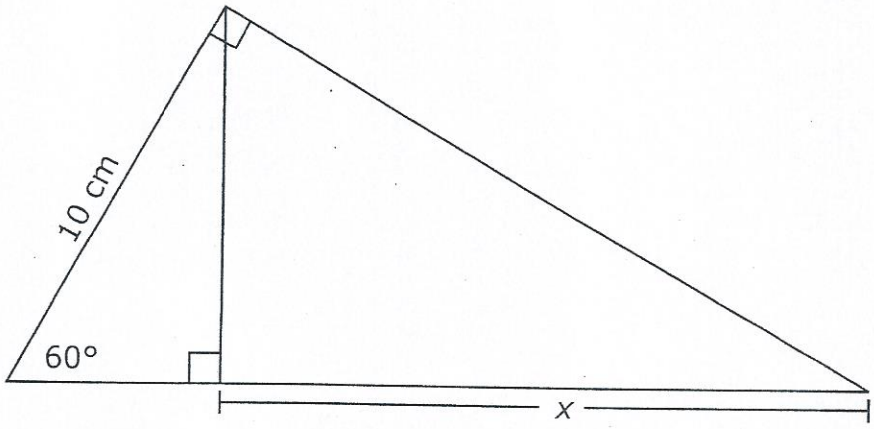
A. $sin^2(\theta) - cos^2(\theta)$

B. $cos^2(\theta) - sin^2(\theta)$

C. 2

D. 1

12. What is the value of x in the triangle below?



A. $\frac{5\sqrt{3}}{2}$ cm B. $5\sqrt{3}$ cm C. 10 cm D. 15 cm

13. Which angle, in standard position, is NOT coterminal with the others?

A. -190^0 B. -170^0 C. 190^0 D. 550^0

14. The diameter of a circle is 8 centimeters. A central angle of the circle intercepts an arc of 12 centimeters. What is the radian measure of the angle?

A. $\frac{3}{2}$ B. 3 C. 4 D. 8π

15. In a circle, an arc of length 8π cm is intercepted by a central angle of $\frac{2\pi}{3}$ radians. What is the radius of the circle?

A. $\frac{3\pi}{16}$ cm B. $\frac{16\pi}{3}$ cm C. $\frac{16\pi^2}{3}$ cm D. 12 cm

16. What is the amplitude of $y = 3\sin 4\theta$?

A. $\frac{4}{3}$ B. 3 C. 4 D. 2π

17. Which answer choice describes $y = -\sin 2\theta$?

A. amplitude -1, period 4π B. amplitude 1, period π

C. amplitude 2, period $-\pi$ D. amplitude 2π, period 1

18. Which function has a period of 4π and an amplitude of 8?

A. $y = -8\sin 8\theta$ B. $y = -8\sin\frac{1}{2}\theta$ C. $y = 8\sin 2\theta$ D. $y = 4\sin 8\theta$

19. Which function is a phase shift of $y = \sin\theta$ by 5 units to the left?

A. $y = 5\sin\theta$ B. $y = \sin\theta + 5$ C. $y = \sin(\theta + 5)$ D. $y = \sin 5\theta$